

# Symbolic Quantitative Information Flow

Quoc-Sang Phan, Pasquale Malacaria  
Queen Mary University of London

Oksana Tkachuk, Corina S. Păsăreanu  
NASA Ames Research Center

## ABSTRACT

*Quantitative Information Flow* (QIF) is a powerful approach to quantify leaks of confidential information in a software system. Here we present a novel method that precisely quantifies information leaks. In order to mitigate the state-space explosion problem, we propose a symbolic representation of data, and a general SMT-based framework to explore systematically the state space. *Symbolic Execution* fits well with our framework, so we implement a method of QIF analysis employing Symbolic Execution.

We develop our method as a prototype tool that can perform QIF analysis for a software system developed in Java. The tool is built on top of Java Pathfinder, an open source model checking platform, and it is the first tool in the field to support information-theoretic QIF analysis.

## 1. INTRODUCTION

Protecting confidential data is always a big concern when building a software system. Intuitively, a system is considered to be secure if confidential data cannot be inferred by an attacker through his observations of the system. This intuitive policy is formalized as *non-interference*: an observable output  $O$  is not affected by any confidential data  $H$ . *Non-interference* has been widely studied during the last four decades [14]. Although satisfying *non-interference* is a sound guarantee for a system to be secure, this classifies many intuitively secure programs as insecure. Consider for example the following password checking program:

```
if (H == L)    accept  else  reject
```

The program takes a public input  $L$  controlled by the user, grants access if  $L$  is equal to the confidential password  $H$ , and rejects otherwise. With a strong enough password, this program is intuitively secure. However, it violates *non-interference* since the result of “accept” or “reject” depends on the confidential data  $H$ . Therefore, qualitative methods would classify the program as insecure. This is the main

weakness of qualitative methods, which makes the analysis imprecise for a large class of programs.

*Quantitative Information Flow* (QIF) has been developed to address the limitation of qualitative information flow [7, 8]. The key idea of QIF is simple: instead of accepting only programs with “zero interference” (*non-interference*) as secure, we quantify the interference and accept programs with “small” interference as secure. To illustrate the concept of QIF, we consider an attacker model in which an attacker observes the program  $P$  and tries to infer the value of the confidential data  $H$  of the program by observing the output  $O$  of  $P$ . Suppose we have a function  $F$  measuring the attacker’s knowledge of the secret. Initially, the knowledge of  $H$  is  $F(H)$ ; we note the attacker’s knowledge about  $H$  after observing the output  $O$  by  $F(H|O)$ . We then define leakage as the difference between the *a priori* and *a posteriori* attacker’s knowledge, i.e.

$$\Delta_F(H) = F(H) - F(H|O)$$

If the program satisfies *non-interference*, observing  $O$  will not affect the attacker’s knowledge of  $H$ :

$$F(H|O) = F(H) \quad \text{thus} \quad \Delta_F(H) = 0$$

In general the security policy is relaxed from 0 to an acceptable threshold  $k$ . This enables QIF to tolerate small leaks and accept more programs as secure.

The function  $F$  is in general based on Information Theory. A natural choice for  $F$ , when interpreting knowledge as information, is Shannon entropy. An alternative, if one views knowledge in terms of the *probability* of guessing the confidential data in one try, is to choose  $F$  as Renyi’s min-entropy [15]. Alternatively,  $F$  can also be guessing entropy [11], if knowledge is interpreted as the *expected number of guesses* to reveal the confidential data. An interesting result is that these three metrics agree in order [9]; it means that for all possible *a priori* knowledge, if program  $P$  leaks less than program  $P'$  when analysing with one of the three metrics, then the result will be the same if we employ the other metrics. Readers who are interested in algebraic foundations of QIF may consult [9, 15] for more details.

## 2. BACKGROUND

There is always a trade-off between precision and computational complexity, and this is the case for QIF. While providing more precision in reasoning about security, QIF also introduces more complexity than traditional qualita-

tive methods. It is impractical to perform QIF analysis manually as in [8] for real-world applications. That leads to the need of automated, possibly approximated, methods for QIF. Previous work [10, 15] has proved that:

$$\Delta_F(H) \leq \log_2(N) \quad (1)$$

with  $N$  as the number of possible values for the output  $O$ . This result is important, since it frees us from the tedious and expensive task of calculating various (conditional) probabilities on software data. Thus, the problem of QIF analysis is reduced to the problem of counting  $N$ . From now on, when we talk about "precise" or "approximate" QIF analysis, we also mean precise or approximate calculation of  $N$ , since precise calculation of  $\Delta_F(H)$  is almost impossible.

However, even if the result in (1) reduces the complexity of a QIF analysis, the problem of an automated analysis is far from being solved: counting the number of possible outputs  $N$  remains a huge challenge. Suppose a program  $P$  takes  $k$  inputs  $I_1, I_2, \dots, I_k$  and produces an output  $O$ .  $P$  can be viewed as a function:

$$f : \mathcal{D}_1 \times \mathcal{D}_2 \times \dots \times \mathcal{D}_k \rightarrow \mathcal{D}_o$$

where  $\mathcal{D}_1, \mathcal{D}_2, \dots, \mathcal{D}_k$  and  $\mathcal{D}_o$  are domains of  $I_1, I_2, \dots, I_k$  and  $O$  respectively. In a simple case where data are 32-bit integers, a domain  $\mathcal{D}_i$  already ranges up to  $2^{31} - 1$ . To count the number of possible outputs, one may be tempted to think of an exhaustive counting as follows:

```

N = 0
for all v in  $\mathcal{D}_o$  do
  if (assert  $O \neq v$  is violated) then
    N ← N + 1
  end if
end for
return N

```

The assertion can be verified by formal methods such as model checking. Assuming we have a very powerful model checking tool that can verify each assertion in one second, the procedure would take around  $2^{32}$  seconds, which is approximately 136 years. In fact, it is easy to prove by Rice's theorem<sup>1</sup> that the problem of counting possible values of a program output is *undecidable*.

The first automated method that could precisely quantify information leaks was proposed by Backes et al. [5]. The method can be divided into two stages: first, it employs model checking to compute an equivalent relation  $\mathcal{R}$  on the set of confidential inputs w.r.t. observable outputs; secondly, if this relation  $\mathcal{R}$  can be represented by a system of *linear integer inequalities*  $A\bar{x} \geq \bar{b}$ , which means it is a bounded integer *polytopes*, then a variant of Barvinok's algorithm [6] can be used to count the number of integer solutions of  $\mathcal{R}$ . While this is an important work as the first effort on automation of QIF analysis, there is little hope that real-world programs will satisfy this condition.

Meng et al. introduce an approximate method, which we call BitPattern, to calculate an upper bound on the number of possible outputs in [12]. The key idea is as follows: if all

<sup>1</sup>[http://en.wikipedia.org/wiki/Rice's\\_theorem](http://en.wikipedia.org/wiki/Rice's_theorem)

possible values of the output  $O$  are very close to each other in the state space, then the bit vectors representing them have a lot of similarities, called *bit patterns*. The authors discover these patterns as a SAT formula, then employing Mathematica [4], a heavyweight commercial #SAT solver, to count the number of solutions, which is an upper bound on the number of possible outputs. The authors restrict themselves to C-like programs without loops, and leave automation of the method for future work.

**Contribution.** In summary, our contributions in this paper are as follows:

1. We propose a novel method for precise QIF analysis.
2. We analyse the BitPattern method, redesign it to make it fully automated and able to handle Java programs.
3. We implement the two methods in an open-source prototyping tool: **jpf-qif**, the first one to support information-theoretic QIF analysis.

### 3. METHODOLOGY

This section describes our method which we call Symbolic Quantitative Information Flow (SQIF).

#### 3.1 A symbolic representation

The key idea behind SQIF is that instead of checking every concrete value one by one, we build a procedure to process multiple values at a time. To do this, we need a representation that can denote a set of values. The way a computer stores data in vectors of bits suggests a symbolic representation that we define as follows: we consider a set of boolean variables  $\Phi := \{p_1, p_2, \dots, p_K\}$ , representing a variable of  $K$  bits in the computer memory. In order to count the models representing possible outputs of program  $P$ , we need a formula  $\Gamma$  such that each model of  $\Gamma$  corresponds to a concrete value of the output  $O$ . We also need a decision procedure *isSAT* to check the satisfiability of  $\Gamma$ .

For a program  $P$  with an output  $O$  of data type of size  $K$ ,  $O$  is stored in the computer memory as a bit vector  $bv_o$  of  $K$  bits:  $bv_o = b_K b_{K-1} \dots b_1$ . We set up  $\Gamma$  as a bijective mapping  $\Gamma : bv_o \rightarrow \Phi$ , which can be implemented by adding the code in Figure 1 to the original program. The symbolic

```

for all element  $b_i$  in vector  $bv_o$  do
  if ( $b_i == 1$ ) then
     $p_i = True$ 
  else
     $p_i = False$ 
  end if
end for

```

**Figure 1: Symbolic representation conversion**

formula  $p_1$  is a shorthand notation for the family of sets  $\{\Phi := \{p_1, p_2, \dots, p_K\} : p_1 = True\}$ . This family of sets can represent up to  $2^{K-1}$  concrete values. Similarly,  $p_1 \wedge \neg p_2$  represents a family of sets representing up to  $2^{K-2}$  concrete values. At this point we have defined the notation of a symbolic representation  $\Phi$  of the state space of the output  $O$ . In the next section, we will describe a DPLL-based<sup>2</sup> framework to systematically explore  $\Phi$ .

<sup>2</sup>[http://en.wikipedia.org/wiki/DPLL\\_algorithm](http://en.wikipedia.org/wiki/DPLL_algorithm)

### 3.2 A symbolic QIF framework

The exhaustive counting procedure discussed in the previous section is inefficient, but intuitive: the only solution for precise counting is searching for all possible solutions. The source of inefficiency is that the procedure checks all concrete values of the data type, while the domain of the output  $O$  is often small (note that we aim to tolerate small leaks, not to quantify the big ones). The symbolic QIF framework we propose here systematically explores the symbolic representation  $\Phi$  of the output, and trims infeasible values in the process. For example, if we discover that  $p_1$  is a tautology, then we can trim  $2^{31}$  concrete values represented by  $\neg p_1$ , thus approximately saving 68 years compared with the exhaustive counting.

A high level framework to explore the state-space and quantify the leaks of confidential data is described in Figure 2. The recursive call *SymCount* is described in Figure 3.  $\Phi$ ,  $\Psi$  and  $N$  are passed by reference, while  $pc$  and  $i$  are passed by value.  $\Phi$  is the symbolic representation described in the previous section, and  $\Psi$  keeps the models of  $\Gamma$  being explored.  $N$  is the cardinality of  $\Psi$ , and the procedure *SymbolicQIF* returns  $\log_2(N)$  as the maximum leakage of confidential data.  $K$  is the size of the data type, e.g.  $K = 32$  if  $O$  is a 32-bit integer, and  $i$  is the depth of the recursive call. In the process of exploring the state-space, the explored predicates are kept in a *trace*, which we name  $pc$  in referring to path condition in symbolic execution, discussed further in the next section;  $pc$  is incrementally updated when the search progresses.

```

function SYMBOLICQIF( $\Phi$ )
   $\Psi \leftarrow \epsilon$ ,  $N = 0$ ,  $i = 1$ 
   $pc \leftarrow \text{InitializePC}()$ 
  SymCount( $\Phi$ ,  $\Psi$ ,  $N$ ,  $pc$ ,  $i$ )
return  $\Psi$ ,  $\log_2(N)$ 
end function

```

Figure 2: Symbolic QIF analysis

```

1: function SYMCOUNT( $\Phi$ ,  $\Psi$ ,  $N$ ,  $pc$ ,  $i$ )
2:   Extract  $p_i$  from  $\Phi$ 
3:    $pc_1 \leftarrow pc \wedge p_i$ 
4:   if (isSAT( $pc_1$ )) then
5:     if ( $i == K$ ) then
6:        $\Psi \leftarrow \Psi \cup \{pc_1\}$ 
7:        $N \leftarrow N + 1$ 
8:     else
9:       SymCount( $\Phi$ ,  $\Psi$ ,  $N$ ,  $pc_1$ ,  $i + 1$ )
10:    end if
11:  end if
12:   $pc_2 \leftarrow pc \wedge \neg p_i$ 
13:  if (isSAT( $pc_2$ )) then
14:    if ( $i == K$ ) then
15:       $\Psi \leftarrow \Psi \cup \{pc_2\}$ 
16:       $N \leftarrow N + 1$ 
17:    else
18:      SymCount( $\Phi$ ,  $\Psi$ ,  $N$ ,  $pc_2$ ,  $i + 1$ )
19:    end if
20:  end if
21: end function

```

Figure 3: Symbolic counting for QIF

At the heart of any QIF method is always a counting technique, and ours is described in the method *SymCount* in Figure 3. To illustrate the technique, we consider a case study of data sanitization from [12], which is shown in Figure 4. All the data are 32-bit integers, the confidential data

```

base = 8;
if ( $H < 16$ )
   $0 = \text{base} + H$ 
else
   $0 = \text{base}$ 

```

Figure 4: A data sanitization program

$H$  is only manipulated if it is in an acceptable range, namely from 0 to 15. However, while manipulating  $H$ , the program leaks information in the process. It is trivial to prove that only integer values from 8 to 23 are possible outputs of this program, i.e. the number of possible outputs  $N = 16$ .

At the beginning, all variables are initialised as in Figure 2, the method *InitializePC* sets  $pc$  as empty. The method *SymCount* is then called to count the number of possible models of  $\Gamma$ . When a variable  $p_i$  is in consideration, we

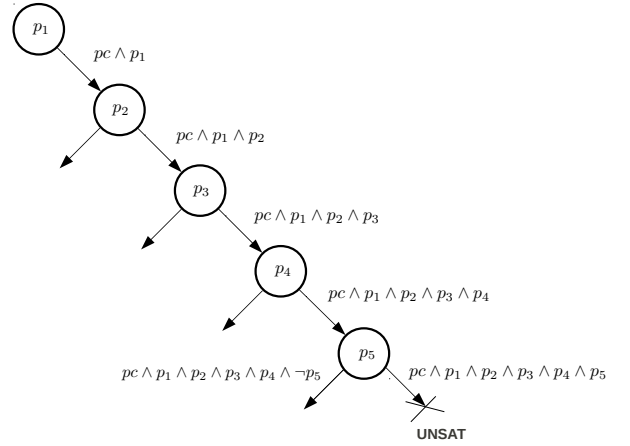


Figure 5: An exploration path of SQIF

systematically explore in the same way for both  $p_i$  and  $\neg p_i$ . Hence, the block of code from line 3 to line 11, and the one from line 12 to line 20 in Figure 4 are symmetric; we only explain the first one.

A trace of the method is described in Figure 5. At the first call of *SymCount*:  $i = 1$ , the variable  $p_1$  is in consideration, SQIF takes one step forward by adding  $p_1$  to the trace like in line 3. Since  $pc$  is initialised to be empty,  $pc_1 = p_1$ . The method *isSAT* is called to check whether  $\Gamma \models p_1$  holds, which can be done by modelling  $\Gamma \models p_1$  as an assertion in a Java program as follows:

```

assert  $p_1$ ;

```

A model checking tool like Java Pathfinder (JPF) [1] can be used to verify this assertion. In this example, *isSAT* would return *True* since all odd values from 9 to 23 are possible outputs satisfying this condition. Therefore, SQIF proceeds by calling *SymCount* with  $i = 2$ . Similarly, the procedure

progresses until calling *SymCount* with  $i = 5$ , which means it needs to verify:

```
assert p1 && p2 && p3 && p4 && p5;
```

This time *isSAT* would return *False*, since  $p_1 \wedge p_2 \dots \wedge p_5$  represents a set of outputs of which each element is at least  $2^0 + 2^1 + \dots + 2^4 = 31$ , while the possible range of  $O$  is only from 8 to 23. For a program with an output of 32-bit integer, namely  $K = 32$ , SQIF trims a set of  $2^{27}$  concrete values represented by the family of sets  $\{\Phi := \{p_1, p_2, \dots, p_{32}\} : p_1 \wedge p_2 \wedge p_3 \wedge p_4 \wedge p_5\}$ . This is how the state-space explosion problem is mitigated.

At the depth  $i = 5$  as above, if SQIF takes the path of  $\neg p_5$  from line 12, then *isSAT* returns *True* ( $O = 15$  is one of the models). Hence, the procedure continues with  $i = 6$ , and from this point until  $i = 32$ , only the path of  $\neg p_i$  is SAT. At  $i = 32$ , SQIF finds a full path 00.01111 which represents an output  $O = 15$ . This path is added to  $\Psi$ , and SQIF increases  $N$ . Finally, at the end of the method *SymbolicQIF*, we have  $\Psi = \{8, 9, \dots, 23\}$  and  $N = 16$ , thus we can conclude that the data sanitization program in Figure 4 leaks at most 4 bits.

## 4. IMPLEMENTATION

We choose to apply our method to programs developed in Java. For Java or C/C++, extracting the  $i^{\text{th}}$  bit from a variable  $O$  is fairly easy:

$$b_i = (O \gg i) \&\& 1 \quad (2)$$

In this way, we can construct the bit vector  $bv_o = b_K b_{K-1} \dots b_1$  for the output  $O$ . The constraint mapping  $\Gamma$  is implemented by adding the code in Figure 1 to the original program as we have already explained. In the previous section, we explained our framework in which *InitializePC* sets  $pc$  to empty, and *isSAT* is implemented by verifying an assertion. However, to implement the framework from scratch is costly, and there is a software analysis technique that comes with a similar idea of using symbols to present sets of concrete values, which is symbolic execution. This technique fits with our framework by nature, so we have adapted it into a QIF analysis tool.

### 4.1 SQIF by Symbolic execution

Symbolic execution (SE) is a hybrid of verifying and testing, which means that it can be either complete or incomplete. In order to use SE as a verifying technique, we assume a bounded model of runtime behaviour, which means programs always terminate and have no recursion, loops can be unfolded and so on. These are well-known issues in symbolic execution and handling them is orthogonal to our work.

In our framework in Figure 4, we name the trace  $pc$  in referring to path condition because of the similarity in the way they are updated. For an **if** statement with condition  $c$ , there are three possible cases: (i)  $pc \vdash c$ : SE chooses the **then** path; (ii)  $pc \vdash \neg c$ : SE chooses the **else** path; (iii)  $(pc \not\vdash c) \wedge (pc \not\vdash \neg c)$ : SE executes both paths: in the **then** path, it updates the path condition  $pc_1 = pc \wedge c$ , in the **else** path it updates the path condition  $pc_2 = pc \wedge \neg c$ . The third case (iii) is interesting to us, since it is similar to how we update the trace  $pc$ . Moreover, for a trace  $pc$ , the first two cases (i) and (ii) cannot occur because when we consider a variable  $p_i$ , the trace only contains variables from  $p_1$  to  $p_{i-1}$ .

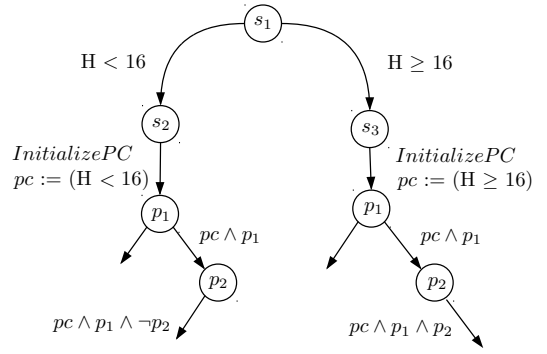


Figure 6: An exploration path of SQIF-SE

In Figure 1, since each bit can take only two possible values, 0 or 1, the way we set up the constraints  $\Gamma$  explicitly imposes the conditions that describe all combination of  $p_i$ . Thus, SE is forced to explore all the state space of  $O$ . SE as implemented in Symbolic Pathfinder (SPF) [13] also returns a concrete value satisfying the path condition. For example, with the condition  $H < 16$  in the program in Figure 4, SPF may return  $H = 1$ . However, a concrete value of the set  $p_1 p_2 \dots p_K$  can represent only one value of  $O$ . Hence, we only need to count the concrete values of  $O$  that SPF generates for the constraints in Figure 1.

The implementation of SQIF by SE, which we call SQIF-SE, is briefly described in Figure 6; the example is still the one that we analysed with the SQIF framework. At the beginning, the trace  $pc$  is not initialised as empty but as the path condition of the program, e.g.  $H < 16$  in this example. For each possible path, we explore the state space of  $O$  as we discussed in the previous section.

### 4.2 Automation of BitPattern method

In order to discover *bit patterns*, Meng et al. [12] transform the program into a set of Static Single Assignment predicates. These predicates are then translated into the language of STP solver [3]. The whole process is performed manually by the authors. Bit patterns are discovered by making queries about the bits of the output  $O$ : for example the following STP query tests whether bit  $i$  of  $O$  is necessarily 0.

```
QUERY( $O[i : i] = 0\text{bin}0$ )
```

We redesign the BitPattern method, and make it fully automated and able to handle Java programs: we extract bits from the output as in (2), then replace the queries about the bits by making assertions about them. For example, the following assertion is logically equivalent to the query above:

```
assert  $b_i == 0$ ;
```

The assertions are checked by JPF. With the case study in Figure 4, BitPattern discovers that the assertion above is valid for  $6 \leq i \leq 32$ . For  $1 \leq i \leq 5$ , neither  $b_i == 0$  nor  $b_i == 1$  are valid. Thus, the bit vectors representing possible outputs of  $O$  have the same pattern: 00..0\*\*\*\*, where a '\*' represents a bit that can be flipped. Also by verifying assertions, BitPattern discovers further that  $b_4 b_5$  together can only take two values 01 or 10. Therefore, the number of solutions for the bit patterns is  $2 \times 2^3 = 16$ .

In general, we transform bit patterns into CNF formula in DIMACS format, then use RelSat [2], a lightweight open-source #SAT solver, to perform model counting.

Both SQIF-SE and BitPattern are implemented in an open-source prototyping tool, **jpf-qif**, as an extension of JPF.

## 5. PRELIMINARY EXPERIMENTS

In the illustrative example in Figure 4, there is a *direct flow* from the confidential data  $H$  to the output  $O$  via assignment. Consider another example in which the program *indirectly* copies  $H$  to  $O$  if  $H \leq 6$  as follows:

```

0 = 0;
if (H == 0) 0 = 0;
else if (H == 1) 0 = 1;
else if (H == 2) 0 = 2;
else if (H == 3) 0 = 3;
else if (H == 4) 0 = 4;
else if (H == 5) 0 = 5;
else if (H == 6) 0 = 6;
else 0 = 0;

```

Meng et al. reported an elapsed time of 45 ms, and BitPattern returns a bound of 3 bits. With the same example, it takes SQIF-SE 717 ms to count 7 possible outputs, and concludes a bound of 2.81 bits.

In previous case studies, BitPattern performs quite accurately when possible outputs are in the same range, e.g. 8..23 and 0..6. Consider a similar case study of a family of programs that each have exactly 10 feasible outputs:

```

if (H == r1) 0 = r1;
else if (H == r2) 0 = r2;
...
else if (H == r9) 0 = r9;
else 0 = r10;

```

When  $r1$  to  $r9$  are generated uniformly and independently, the possible outputs diverge in the state space: BitPattern greatly overestimates the bound on information leakage. With 20 such programs, Meng et al. reported an average result of a bound of 18.645 bits in 5 seconds. On the other hand, SQIF-SE always finds exactly 10 outputs in around 1 second, which results in a bound of 3.322 bits.

## 6. CONCLUSION

In this paper we propose SQIF, a novel method to mitigate the state-space problem in QIF analysis. We have built **jpf-qif**, the first tool to support information theoretic QIF analysis. Compared with the precise QIF analysis in [5], SQIF can handle non-linear relations of various data types. Compared with BitPattern, SQIF is always more precise, but it is slower when leaks are in the same range. In contrast, SQIF is better in both effectiveness and efficiency when leaks diverge in the state space. An immediate direction for investigation is to combine SQIF with a cheap qualitative method, e.g. type system, to decide quickly if the program satisfies *non-interference*. This will improve the efficiency of the tool when programs are strictly secure.

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